

COLLEEN FLOATING POINT ROUTINES BY C SHAW

for Harry

TITLE 'COLLEEN FLOATING POINT ROUTINES BY C SHAW'

MORE ACCURATE VERSIONS OF THE FOLLOWING SHEPARDSON ROUTINES

EXP, EXP10, LOG, LOG10, SIN, COS, ATAN, SQR AND POWER

THESE ROUTINES WERE TAKEN FROM THE CALCULATOR CARTRIDGE AND MODIFIED
MANY OTHER MATH FUNCTIONS SUCH AS TAN, ARCSIN AND ARCCOS ARE ALSO
INCLUDED IN THAT CARTRIDGE.

0075	CR	=	\$9B	; ATASCII CARRIAGE RETURN
0005	GETREC	=	5	; GET RECORD
0009	PUTREC	=	9	; PUT RECORD
0342	ICOM	=	\$342	
0344	ICBAL	=	\$344	
0348	ICBL	=	\$348	
E456	CIOV	=	\$E456	

FLOATING POINT SUBROUTINES

0006	FPREC	=	6	; FLOATING PT PRECISION (# OF BYTES)
D800	AFP	=	\$DB80	; IF CARRY USED THEN CARRY CLEAR => NO ERROR, CARRY SET => ERROR
				; ASCII->FLOATING POINT (FP)
D8E6	FASC	=	\$DBE6	INBUFF+CIX -> FRO, CIX, CARRY
D9AA	IFP	=	\$D9AA	; FP -> ASCII FRO-> LBUFF (INBUFF)
				; INTEGER -> FP
D9D2	FPI	=	\$D9D2	0-\$FFFF (LSB, MSB) IN FRO, FRO+1->FRO
DA60	FSUB	=	\$DA60	; FP -> INTEGER FRO -> FRO, FRO+1, CARRY
DA66	FADD	=	\$DA66	FRO <- FRO + FR1 , CARRY
DADB	FMUL	=	\$DADB	FRO <- FRO * FR1 , CARRY
DB28	FDIV	=	\$DB28	FRO <- FRO / FR1 , CARRY
DD89	FLDOR	=	\$DD89	FLOATING LOAD REG0 FRO <- (X, Y)
DD98	FLDIR	=	\$DD98	; " " REG1 FR1 <- (X, Y)
DDA7	ESTOR	=	\$DDA7	FLOATING STORE REG0 (X, Y) <- FRO
DDB6	FMOVE	=	\$DBB6	FR1 <- FRO
DD40	PLYEV	=	\$DD40	FRO <- P(Z) = SUM(I=N TO 0) (A(I)*Z**I) CARRY
				INPUT: (X, Y) = A(N), A(N-1)...A(0) -> PLYARG
				ACC = # OF COEFFICIENTS = DEGREE+1
				FRO = Z
DDC0	EXP	=	\$DDC0	FRO <- E**FRO = EXP10(FRO * LOG10(E)) CARRY
DDCC	EXP10	=	\$DDCC	FRO <- 10**FRO CARRY
DEC0	LOG	=	\$DEC0	FRO <- LN(FRO) = LOG10(FRO)/LOG10(E) CARRY
DED1	LOG10	=	\$DED1	FRO <- LOG10 (FRO) CARRY
				THE FOLLOWING ARE IN BASIC CARTRIDGE
	SIN	=	\$DB81	FRO <- SIN(FRO) DEGFLG=0 => RADS, 6=>DEG CARRY
	COS	=	\$BD73	FRO <- COS(FRO) CARRY
	ATAN	=	\$BE43	FRO <- ATAN(FRO) CARRY
	SQR	=	\$BEB1	FRO <- SQUAREROOT(FRO) CARRY

; FLOATING POINT ROUTINES ZERO PAGE (NEEDED ONLY IF F.P. ROUTINES ARE CALLED)

00D4	FRO	=	+\$D4	
00DA	FRE	=	+\$D4	
00E0	FR1	=	+\$D4	
00E6	FR2	=	+\$D4	

FLOATING POINT ROUTINES ZERO PAGE (NEEDED ONLY IF F.P. ROUTINES ARE CALLED)

0004	FRX	*=-*+1	
0005	FRX	*=-*+FPREC	; FP RECD
0006	FRX	*=-*+FPREC	; FP REQD
0007	FRX	*=-*+FPREC	

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00E0	FRX	*=-*+1	; FP SPARE
00E1	ELFR	*=-*+1	; VALUE OF E
00E2	NSIGN	*=-*+1	; SIGN OF #
00E3	ESIGN	*=-*+1	; SIGN OF EXPONENT
00F0	FCMRFLG	*=-*+1	; 1ST CHAR FLAG
00F1	DIGRT	*=-*+1	; # OF DIGITS RIGHT OF DECIMAL
00F2	DXK	*=-*+1	; CURRENT INPUT INDEX
00F3	INBUFP	*=-*+2	; POINTS TO USER'S LINE INPUT BUFFER
00F5	ZTEMP1	*=-*+2	
00F7	ZTEMP4	*=-*+2	
00F9	ZTEMP3	*=-*+2	
00FB	RADFLC	*=-*+1	; 0=RADIANS, 6=DEGREES
00FD	FLPTR	*=-*+2	; POINTS TO USER'S FLOATING PT NUMBER
00FE	FFTR	*=-*+2	

FLOATING PT ROUTINES' NON-ZERO PAGE RAM (NEEDED ONLY IF F.P. ROUTINES CALLED)

057E	LBPR1	*=-*+1	; LBUFF PREFIX 1
057F	LBPR2	*=-*+1	; LBUFF PREFIX 2
0580	LBUFF	*=-*+128	; LINE BUFFER
05E0	PLYARG	=	LBUFF+\$60 ; POLYNOMIAL ARGUMENTS
05E6	FPSCR	=	PLYARG+FPREC
05EC	FPSCR1	=	FPSCR+FPREC
05E6	FSCR	=	FPSCR
05EC	FSCR1	=	FPSCR1

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000B	NATCF	=	\$B
0006	NSDF	=	6
D905	FASC2	=	\$D905
D920	XEFORM	=	\$D920
D928	XEFRM2	=	\$D928
DA44	ZFRO	=	\$DA44
DA46	ZF1	=	\$DA46
DA51	INTLBF	=	\$DA51
DC00	NORM	=	\$DC00
DC70	XCVFRO	=	\$DC70
DE03	EXP1	=	\$DE03
DE12	EXP11	=	\$DE12
DE89	LOG1OE	=	\$DEB9
DE95	XFORM	=	\$DE95
DF6C	FHALF	=	\$DF6C
DFAE	ATCOEF	=	\$DFAE
DFFA	FP9S	=	\$DFFA
DFF0	PIOV4	=	\$DFF0

FP PACKAGE EQUATES FOR SIN, COS, ATAN, AND SQR ROUTINES ETC

; NUMBER OF ATAN COEFFICIENTS FOR POLYNOMIAL EVALUATION
; NUMBER OF SIN COEFFICIENTS
;
; AFTER FASC (FINISH FP TO ASCII CONVERSION)
; !EFORM PROCESS E FORMAT FOR FP -> ASCII CONVERSION
; AFTER XEFORM (FINISH CONVERSION)
; FRO <- 0
; CLEAR 6 BYTES STARTING AT 0,X
; INIT LBUFF INTO INBUFF FOR FP -> ASCII CONVERSION
; NORMALIZE FLOATING POINT NUMBER - USED BY STRUNC ONLY
; !CVFRO FP TO 10 ASCII DIGITS IN LBUFF
; MIDDLE OF EXP10 WHERE PLYEVL IS CALLED
; AFTER PLYEVL IN EXP10
; LOGTEN(E) = .4342944819
; FRO <- (FRO-(X,Y)) / (FRO+(X,Y))
; FLOATING POINT CONSTANT .5
; ATAN COEFFICIENTS
; FLOATING POINT CONSTANT .9999999999 (ALMOST 1)
; FLOATING POINT CONSTANT PI/4 = .7853981634

VARIABLES

0480	**=\$480	
0481	QUADFLG **=**+1	; SIN QUADRANT FLAG
0481	INTFLG **=**+1	; FLAG FOR POWER ROUTINE
0482	FTEMP **=**+6	; TEMPORARY FLOATING POINT REGISTER FOR POWER ROUTINE

COLLEEN FLOATING POINT ROUTINES BY C SHAW

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*=A000          ; ARBITRARY STARTING POINT

TEST PROGRAM

A000      START
A000 20 4C A0  JSR    GETNUM
A003 20 B6 DD  JSR    FMOVE
A006 20 4C A0  JSR    GETNUM ; GET 2ND NUMBER FROM E: -- OMIT IF ONLY ONE ARGUMENT
A009 20 CE A0  JSR    SPPOWER ; CHANGE TO GET DIFFERENT ROUTINES
A00C 90 OA     BCC    NOERR

; ERROR -- DISPLAY MESSAGE

A00E A9 79      LDA    #ERRMSG
A010 BD 44 03   STA    ICBAL
A013 A9 A0      LDA    #ERRMSG/256
A015 4C 32 A0   JMP    CONTIN

A018      NOERR
A018 20 E6 DB   JSR    FASC   ; FLOATING POINT TO ASCII
; FIND END OF STRING AND CHANGE NEGATIVE # TO POSITIVE AND ADD CARRIAGE RETURN.

A01B AO FF      LDY    #$FF
A01D C8         MLOOP
A01D CB
A01E B1 F3      INY
A020 10 FB      LDA    (INBUFF), Y
A022 29 7F      BPL    MLOOP
A024 91 F3      AND    #$7F
A026 C8         STA    (INBUFF), Y
A027 A9 9B      INY
A029 91 F3      LDA    #CR
                      STA    (INBUFF), Y

; DISPLAY RESULT

A02B A5 F3      LDA    INBUFF
A02D BD 44 03   STA    ICBAL
A030 A5 F4      LDA    INBUFF+1
A032      CONTIN
A032 BD 45 03   STA    ICBAL+1
A035 A9 09      LDA    #PUTREC
A037 BD 42 03   STA    ICCOM
A03A A9 28      LDA    #40
A03C BD 48 03   STA    ICBLL
A03F A9 00      LDA    #0
A041 BD 49 03   STA    ICBLL+1
A044 A2 00      LDX    #0
A046 20 56 E4   JSR    CIOV

A049 4C 00 A0   JMP    START ; DO IT AGAIN

A04C      GETNUM
A04C A9 05      LDA    #GETREC
A04E BD 42 03   STA    ICCOM ; GET ONE NUMBER FROM E: (IOCB #0)
                                ; GET RECORD (ENDS IN CR)

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A04C GETNUM , GET ONE NUMBER FROM E (IOCB #0)
A04C A9 05 #GETREC ; GET RECORD (ENDS IN CR)
A04E BD 42 03 ICOMM

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A051 A9 80	LDA	#LBUFF
A053 BD 44 03	STA	ICBAL
A055 A9 05	LDA	#LBUFF/256
A058 BD 45 03	STA	ICBAL+1
A05D A9 28	LDA	#40
A05D BD 48 03	STA	ICBLL
A060 A9 00	LDA	#0
A062 BD 49 03	STA	ICBLL+1
A065 A2 00	LDX	#0
A067 20 56 E4	JSR	CIOV
A06A A9 80	LDA	#LBUFF
A06C 85 F3	STA	INBUFF
A06E A9 05	LDA	#LBUFF/256
A070 85 F4	STA	INBUFF+1
A072 A9 00	LDA	#0
A074 85 F2	STA	CIX
A076 4C 00 DB	JMP	AFP

; CALL ASCII TO FLOATING POINT AND RETURN

A079 45 52 52 ERRMSG BYTE "ERROR", CR ; INDICATES CARRY SET RETURN FROM FP ROUTINE
A07C 4F 52 9B

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FRO <- E^FRO

USES INTEGER FUNCTION LIKE BASIC'S INSTEAD OF JUST IFP, WHICH ROUNDS
PROVIDES ACCURACY OF AT LEAST 7 DIGITS (EXCEPT POSSIBLY AT EXTREMA)
INSTEAD OF 6.

A07F      SEXPE
A07F A2 B9    LDX #LOG1OE      ; E^X (SEE SHEP ATARI BASIC $DDCO EXP)
A081 AO DE    LDY #LOG1OE/256   ; E^X = 10^(X*LOGTEN(E))
A083_20 E8 A2  JSR LD1MUL     ; FRO <- FRO*LOG1OE

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FRO <- 10^FRO      (SEE COMMENTS FOR SEXPE)

RETURNS EXACT POWER OF 10 FOR INTEGERS.

A086      SEXPTE
A086 A9 00    LDA #0          ; 10^X (SEE SHEP ATARI BASIC $DDCC EXP10)
A088 B5 F1    STA DIGRT      ; CLEAR TRANSFORM FLAG
A08A A5 D4    LDA FRO        ; XFMFLG
A08C B5 F0    STA FCHRFLG    ; SAME AS SGNFLG  REMEMBER ARG SIGN
A08E 20 D2 A2  JSR SAD5VA    ; TAKE ABSOLUTE VALUE, AC-FRO
A091 38
A092 E9 40    SBC #$40
A094 30 27    BMI SEXPO5    ; X<1 SO USE SERIES DIRECTLY (BUT CHECK FOR 0 FIRST)
A096 A2 E6    LDX #FPSCR
A098 A0 05    LDY #FPSCR/256
A09A 20 A7 DD  JSR FSTOR    ; SAVE IN SCRATCH REG
A09D 20 18 A3  JSR SINTEG   ; GREATEST INTEGER <= X
A0A0 20 D2 D9  JSR FP1       ; MAKE INTEGER
A0A3 B0 27    BCS SFERR3    ; RETURN IF ERROR
A0A5 A5 D5    LDA FRO+1    ; CHECK MSB
A0A7 D0 23    BNE SFERR3    ; SHOULDN'T HAVE ANY -- RETURN IF ERROR
A0A9 A5 D4    LDA FRO
A0AB B5 F1    STA DIGRT    ; XFMFLG      SAVE MULTIPLIER EXP
A0AD 20 AA D9  JSR IFP       ; NOW TURN IT BACK TO FP
A0B0 20 B6 DD  JSR FMOVE    ; FR1 <- FRO
A0B3 A2 E6    LDX #FPSCR
A0B5 A0 05    LDY #FPSCR/256
A0B7 20 B9 DD  JSR FLDOR    ; RELOAD FROM TEMP SCRATCH REG
A0B8 20 07 A3  JSR SFSUB
A0BD      SEXPOS
A0BF D0 08    LDA FRO
A0C1 A9 01    BNE SEXP10   ; 10^0 = 1
A0C3 20 53 A3  LDA #1
A0C6 4C 12 DE  JSR PSETO
A0C9 4C 03 DE  JMP EXP11    ; $DE12 DO 10^X, SKIPPING PLYEVN  LDA XFMFLG
A0CC      SFERR3
A0CC 3B      SEC
A0CD 60      INIT RTS

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MILLER FLOATING POINT ROUTINE BY C SHAW

FR0 <= FR0 = FR1 = SEXPTE (FR1 * SLOGTE (FR0))

USES MORE ACCURATE SEXPTE INSTEAD OF EXP10
 RETURNS EXACT INTEGER IF BOTH FR0 AND FR1 ARE POSITIVE INTEGERS.
 RETURNS RECIPROCAL OF INTEGER IF BOTH ARE INTEGERS AND FR1 < 0
 RETURNS CARRY SET IF FR0 < 0 OR (FR0 = 0 AND FR1 < 0) OR OVERFLOW.
 $O \wedge FR1 = 0 \text{ IF } FR1 = 0$
 $O \wedge O = 1$

ABCE	SP0WCB	LDA	FR0	; FR0 = 0? / NO / YES.
A0C2 A5 04				
A0D0 B0 00		ENE	SP0W20	
A0D2 A7 00		LDA	#0	
A0D4 A6 E0		LDX	FR1	
A0D6 30 78		BMI	PERR2	; FR1 < 0 $O \wedge -X \Rightarrow \text{ERROR}$
A0D8 D0 02		BNE	SP0W10	; FR1 > 0 $O \wedge X = 0$
A0DA A9 01		LDA	#1	; FR1 = 0 $O \wedge O = 1$
A0DC 4C 53 A3	SP0W10	JMP	PSET0	
A0DF	SP0W20			
A0E1 A5 E0		LDA	FR1	
A0E1 48		PHA		; SAVE FR1'S SIGN
A0E2 29 7F		AND	#\$7F	; TAKE ABSOLUTE VALUE OF FR1
A0E4 B9 E0		STA	FR1	
A0E6 A2 B2		LDX	#FTEMP	; SAVE FR1 IN FTEMP
A0E8 A0 04		LDY	#FTEMP/256	
A0EA 20 D9 A2		JSR	FST1R	
A0ED 20 B6 DD		JSR	FMOVE	
A0F0 A9 01		LDA	#1	
A0F2 BD B1 04		STA	INTFLG	; ASSUME NOT BOTH INTEGERS
A0F3 20 31 A3		JSR	STRUNC	; TRUNCATE FR0 -- RETURN A=0 AND EG IF FR0 WAS ALREADY AN INTEGER
A0FB D0 0F		BNE	SP0W50	; FR0 WAS NOT AN INTEGER
A0FA A2 82		LDX	#FTEMP	; LOAD SAVED VALUE INTO FR0
A0FC A0 04		LDY	#FTEMP/256	
A0FE 20 89 DD		JSR	FLDOR	
A101 20 31 A3		JSR	STRUNC	; TEST FOR INTEGER
A104 D0 03		BNE	SP0W50	; NOT INTEGER
A106 BD B1 04		STA	INTFLG	; O => BOTH INTEGER => RESULT SHOULD BE INTEGER
A109	SP0W50			
A109 A2 E0		LDX	#FR1	
A10B A0 00		LDY	#FR1/256	; FR0 <- FR1 (MOVE ORIGINAL FR0 BACK)
A10D 20 89 DD		JSR	FLDOR	
A110 20 5B A1		JSR	SLOGTE	; LOG10(FR0)
A113 B0 3A		BCS	PERROR	; ERROR => POP FR1 SIGN AND RETURN
A115 A2 B2		LDX	#FTEMP	; LOAD FR1 AGAIN
A117 A0 04		LDY	#FTEMP/256	
A119 20 98 DD		JSR	FLD1R	
A11C 20 DB DA		JSR	FMUL	; FR0 <- FR1 * LOG10(BASE)
A11F B0 2E		BCS	PERROR	; RETURN IF ERROR
A121 20 B6 A0		JSR	SEXPTE	; 10^X FR0
A124 B0 29		BCS	PERROR	
A126 AD B1 04		LDA	INTFLG	; SHOULD RESULT BE INTEGER?
A127 D0 15		BNE	SP0W80	; NO.
				; YES — ROUND TO NEAREST INTEGER
A128 A2 6C		LDX	#HALF	; FR1 <- 0.5
A12D A0 DF		LDY	#HALF/256	
A12F 20 98 DD		JSR	FLD1R	
A132 A5 D4		LDA	FR0	
A134 10 04		BPL	SROUT0	

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A134 A9 0F	LDA	#\$0F+\$00	; IF FRO < 0 THEN FR1 <- -0.5
A135 3D E0	STA	FRI	
A136	SWDNUO		
A138 20 F7 A2	JSR	SFADD	; FRO <- FRO + FR1 (2-LEVEL RETURN IF ERROR)
A13D 20 31 A3	JSR	STRUNC	; TRUNCATE
A140	BPOHBO		
A140 10	CLC		; INDICATE NO ERROR?
A141 68	PLA		; RELOAD FR1'S ORIGINAL SIGN
A142 10 0D	BPL	PRTN	; DONE IF > 0
A143 20 B6 0D	JSR	FMOVE	; IF < 0 THEN TAKE RECIPROCAL
A147 A9 01	LDA	#1	
A149 30 53 A3	JSR	PSETO	; FRO <- 1
A14C 4C 2B 0B	JMP	FDIV	
A14E	PEROR		
A14F 58	PLA		; DISCARD FR1'S SIGN
A150	PERRE		
A150 36	SEC		; INDICATE ERROR
A151	PRTRU		
A151 60	RTS		

COLLEEN FLOATING POINT ROUTINES BY C SHAW

FRO <- NATURAL LOG (FRO)

RETURNS CARRY SET IF FRO<=0
RETURNS EXACTLY 0 IF FRO = 1

A152 R1N JSR LOGCHK ; CHECK FOR 0,1 (SPECIAL CASES)
A152 20 5E A1 JMP LOG
A155 4C CD DE

FRO <- COMMON LOG (FRO) (LOG BASE 10)

SIMILAR TO SLN

A158 SLOCITE
A158 20 5E A1 JSR LOGCHK
A158 4C D1 DE JMP LOG10

A15E LOGCHK SEC ; CHECK FOR 0,1
A15E 38 LDA FRO
A15F A5 D4 CMP ONE, X ; LN(0), LOG(0) => ERROR
A161 F0 13 BEQ PULRTN ; <0 => ERROR => 2-LEVEL RETURN
A163 30 11 BMI PULRTN
A165 A2 05 LDX #FPREC-1

A167 LOGCLP LDA FRO, X
A167 B5 D4 CMP ONE, X
A169 DD A9 A3 BNE RTURN2 ; NOT 1 => OK
A16C D0 0A BNE RTURN2 ; NOT 1 => OK
A16E CA DEX
A16F 10 F6 BPL LOGCLP
A171 68 PLA ; SKIP LOGCHK RETURN
A172 68 PLA
A173 4C 51 A3 JMP PCLRO ; LN(1)=LOGTEN(1)=0
A176 PULRTN PLA
A176 68 PLA
A177 68 PLA
A178 60 RTURN2 RTS

COLLEEN FLOATING POINT ROUTINES BY C SHAW

BASIC SINE & COS ROUTINES

TO FIX BUGS OF VERSION 5.9 OF SHEP BASIC

BY DAVE & LARRY -- MODIFIED BY CAROL
4-6-79

MOD FUNCTION MAKES ROUTINES MORE ACCURATE FOR ANGLES > 360 DEGREES

COSINE ROUTINE -- ADD 90 OR PI/2 TO FRO TO DO SIN

A179	JSR SINMOD	; TAKE ANGLE MOD 2*PI, 360
A179 20 6F A3	JSR PIVDL	; SET UP X & Y REGS TO LOAD PI/2 OR 90
A17C 20 A0 A3	JSR FLD1R	PUT PI/2 OR 90 INTO FR1
A17F 20 9B DD	JSR SFADD	FRO=FRO + PI/2 (OR 90)
A182 20 F7 A2		

SINE ROUTINE

COMPUTE QUADRANT, GET FRACTION AND DO POLYNOMIAL,
THEN ADJUST FOR QUADRANT

A185	JSR SINMOD	; TAKE ANGLE MOD 2*PI, 360
A185 20 6F A3		

A188 20 A0 A3	JSR PIVDL	; LOAD X & Y REGS TO GET PI/2 OR 90
A188 20 0F A3	JSR LD1DIV	FRO=FRO/FR1

NOW HAVE 0-4 (NOT NECESSARILY INTEGER)
IF FRO NOW FRACTION, IT IS QUADRANT 0

A18E A9 00	LDA #0	
A190 8D 80 04	STA QUADFLG	ASSUME QUADRANT 0
A193 A5 D4	LDA FRO	GET EXPONENT
A195 C9 40	CMP #\$40	SUBTRACT 64 EXCESS
A197 90 19	BCC SINF3	GO IF QUADRANT 0

A199 A5 D5	LDA FRO+1	; SHOULD BE 0, 1, 2, OR 3
A19B 8D 80 04	STA QUADFLG	NOW HAVE QUADRANT (0, 1, 2, OR 3)

A19E 20 B6 DD	JSR FMOVE	; FR1 <- FRO
A1A1 20 31 A3	JSR STRUNC	; TRUNCATE FRO
A1A4 20 07 A3	JSR SFSUB	; FRO <- TRUNC(FRO)-FRO
A1A7 20 28 A3	JSR SCHGSG	; CHANGE SIGN -- FRACTIONAL PART (FRO) = FRO - TRUNC (FRO)

A1AA 4E 80 04	LSR QUADFLG	IS IT ODD QUADRANT?
A1AD 90 03	BCC SINF3	NO
A1AF 20 FD A2	JSR ONESUB	; FRO <- 1-FRO

A1B2	SINF3	; SAVE ARG FOR LATER
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A1B2 A2 E6	LDX #FPSCR	
A1B4 A0 05	LDY #FPSCR/256	
A1B6 20 A7 DD	JSR FSTOR	; FPSCR <- FRO

NOW COMPUTE SINE

THIS CODE TAKEN FROM BASIC 5.9 LINES 6760-6770

A1B9 20 EE A2	JSR SSQUR	FRO=X**2
A1BC A9 06	LDA #NSCF	
A1BE A2 AF	LDX #SCDEF	
A1C0 A0 A3	LDY #SCDEF/256	

A1BC A9 06 LDA #NSCF
A1BE A2 AF LDX #SCDEF
A1CO A0 A3 LDY #SCDEF/256

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A1C2 20 40 DD JSR PLYEVL EVALUATE P(X**2)
A1C5 A2 E6 LDX #FPSCR
A1C7 A0 05 LDY #FPSCR/256
A1C9 20 E8 A2 JSR LD1MUL FRO=SIN(X)=X*P(X**2)

; IF LOWER QUADRANT (2 OR 3) THEN FRO=-(FRO)
A1CC 4E 80 04 LSR QUADFLG IS IT LOWER QUAD?
A1CF 90 03 BCC SINF4 NO
A1D1 20 28 A3 JSR SCHGSG ; YES

A1D4 SINF4

; IF ABS(FRO) >= 1 THEN SET TO 1
A1D4 A5 D4 LDA FRO
A1D6 29 7F AND #\$7F WITHOUT SIGN BIT
A1DB C9 40 CMP #\$40 COMPARE \$40
A1DA 90 07 BCC SINFIN
A1DC A9 00 LDA #0
A1DE 85 DB STA FRO+4 ; PERFORM PSEUDO INT(FRO) (CLEAR LAST 2 BYTES)
A1EO B5 D9 STA FRO+5
A1E2 18 SINFN2 CLC ; NO ERROR
A1E3 60 SINFN RTS

COLLEEN FLOATING POINT ROUTINES BY C SHAW

FRO ← ARC TANGENT (FRO)

FROM SHEPARDSON ATARI BASIC 5.9 4-5-79 (MODIFIED)
SAME ACCURACY AS SHEP VERSION -- USES FEWER BYTES

A1E4	SATAN	LDA #0	
A1E4 A9 00		STA FCHRFLG	; SIGN FLAG OFF
A1E6 85 F0		STA DIGRT	; AND TRANSFORM FLAG
A1E8 85 F1		LDA FRO	
A1EA A5 D4		TAX	
A1EC AA		AND #\$7F	
A1ED 29 7F		CMP #\$40	; CHECK X VS 1.0
A1EF C9 40		BMI ATAN1	; X<1 - USE SERIES DIRECTLY
A1F1 30 10		STA FRO	; FORCE PLUS
A1F3 85 D4		TXA	; OLD FRO WITH SIGN
A1F5 8A		AND #\$80	
A1F6 29 80		STA FCHRFLG	; REMEMBER SIGN
A1FB 85 F0		INC	
A1FA E6 F1		DIGRT	
A1FC A2 EA		LDX #FP95	
A1FE A0 DF		LDY #FP95/\$100	
A200 20 95 DE		JSR XFORM	; CHANGE ARG TO (X-1)/(X+1)
A203	ATAN1		
A203 A2 E6		LDX #FPSCR	ARCTAN(X), -1<X<1 BY SERIES APPROX
A205 A0 05		LDY #FPSCR/256	; CAN'T USE FTEMP BECAUSE SATAN IS CALLED BY OTHER ROUTINES WHICH USE IT
A207 20 A7 DD		JSR FSTOR	
A20A 20 EE A2		JSR SSQUAR	; X*X → FRO
A20D A9 0B		LDA #NATCF	
A20F A2 AE		LDX #ATCOEF	
A211 A0 DF		LDY #ATCOEF/256	
A213 20 40 DD		JSR PLYEVL	; P(X*X)
A216 B0 26		BCS ATNOUT	; ERROR
A21B A2 E6		LDX #FPSCR	
A21A A0 05		LDY #FPSCR/256	
A21C 20 E8 A2		JSR LD1MUL	; X*P(X*X)
A21F A5 F1		LDA DIGRT	; WAS ARG XFORMED
A221 F0 10		BEG ATAN2	; NO.
A223 A2 F0		LDX #PIOV4	; YES-ADD ARCTAN(1) = PI/4
A225 A0 DF		LDY #PIOV4/256	
A227 20 98 DD		JSR FLD1R	
A22A 20 66 DA		JSR FADD	
A22D A5 F0		LDA FCHRFLG	; GET ORG SIGN
A22F 05 D4		ORA FRO	
A231 85 D4		STA FRO	; ATAN(-X) = -ATAN(X)
A233	ATAN2		
A233 A5 FB		LDA RADFLG	; RAD OR DEG
A235 F0 07		BEG ATNOUT	; RAD - FINI
A237 A2 D9		LDX #PIOV18	
A239 A0 A3		LDY #PIOV18/256	; DIVIDE BY PI/180 TO CONVERT TO DEGREES
A23B 20 0F A3		JSR LD1DIV	
A23E	ATNOUT	RTS	
A23E 60			

COLLEEN FLOATING POINT ROUTINES BY C SHAW

```

1 FRO C- SQUARE ROOT (FRO)
2
3 FROM SHEPARDSON ATARI BASIC 5.9 4-5-79 (MODIFIED)
4 SAME ACCURACY AS SHEP VERSION -- USES FEWER BYTES
5
6 USES NEWTON-RAPHSON ITERATION
7 F(Y) = Y*Y - X
8 FPRIME(Y) = 2*Y
9 Y[I+1] = Y[I] - F(Y[I]) / FPRIME(Y[I]) = Y[I] + .5*((X/Y[I])-Y[I])
10
11 ERROR EXIT
12
13 A23F          SQRERR
14 A23F 38
15 A240 60
16
17           SEC
18           RTS
19
20           ENTRY POINT
21
22 A241          SSQRT      ; X<-SQRT(X)
23 A241 A2 E0    LDX #FR1
24 A243 20 46 DA JSR ZF1      ; FR1 <- ALL 0'S
25 A246 A2 00    LDX #0
26
27 A248 86 F1    STX DIGRT
28 A24A E8      INX             ; 1
29 A24B 86 E1    STX FR1+1
30 A24D A5 D4    LDA FRO
31 A24F 30 EE    BMI SQRERR   ; ERROR IF <0
32 A251 C9 3F    CMP #$3F
33 A253 F0 09    BEQ FSQR     ; X IN RANGE OF APPROX - GO DO IT TO IT
34 A255 AA      TAX
35 A256 EB      INX
36 A257 86 E0    STX FR1
37 A259 86 F1    STX DIGRT
38 A25B 20 28 DB JSR FDIV     ; X/100**N
39 A25E          FSGR       ; SQR(X) 0. 1<=X<1
40 A25E A9 06    LDA #6
41 A260 85 EF    STA ESIGN
42 A262 A2 E6    LDX #FSCR
43 A264 A0 05    LDY #FSCR/256
44 A266 20 A7 DD JSR FSTOR    ; STASH X IN FSCR
45 A269 A9 02    LDA #2
46 A26B 20 FF A2 JSR INTSUB   ; 2-X
47 A26E A2 E6    LDX #FSCR
48 A270 A0 05    LDY #FSCR/256
49 A272 20 E8 A2 JSR LD1MUL   ; X*(2-X) : 1ST APPROX
50 A275          SQRLP
51 A275 A2 EC    LDX #FSCR1
52 A277 A0 05    LDY #FSCR1/256
53 A279 20 A7 DD JSR FSTOR    ; Y->FSCR1
54 A27C 20 B6 DD JSR FMOVE    ; Y->FR1
55 A27F A2 E6    LDX #FSCR
56 A281 A0 05    LDY #FSCR/256
57 A283 20 B9 DD JSR FLDOR
58 A286 20 28 DB JSR FDIV     ; X/Y
59 A289 A2 EC    LDX #FSCR1
60 A28B A0 05    LDY #FSCR1/256
61 A28D 20 9B DD JSR FLD1R
62 A290 20 60 DA JSR FSUB     ; (X/Y)-Y
63 A293 A2 60    LDX #HALF

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COLLEEN FLOATING POINT ROUTINES BY C SHAW

A295 A0 DF	LDY	#FHALF/256	
A297 20 EB A2	JSR	LDIMUL	i. 5*((X/Y)-Y)=DELTAY
A29A A5 D4	LDA	FRO	; DELTA 0
A29C F0 OE	BEQ	SQRDON	
A29E A2 EC	LDX	#FSCR1	
A2A0 A0 05	LDY	#FSCR1/256	
A2A2 20 98 DD	JSR	FLD1R	
A2A5 20 66 DA	JSR	FADD	; Y=Y+DELTA Y
A2A8 C6 EF	DEC	ESIGN	; COUNT & LOOP
A2AA 10 C9	BPL	SQRLP	
A2AC	SQRDON		
A2AC A2 EC	LDX	#FSCR1	; DELTA = 0 - GET Y BACK
A2AE A0 05	LDY	#FSCR1/256	
A2B0 20 89 DD	JSR	FLDOR	
A2B3 A2 E0	LDX	#FR1	WAS ARG TRANSFORMED?
A2B5 20 46 DA	JSR	ZF1	
A2B8 A5 F1	LDA	DIGRT	; FR1 <- ALL 0'S AGAIN
A2BA F0 16	BEQ	SABSV	
A2BC 38	SEC		; NO FINI
A2BD E9 40	SBC	##\$40	
A2BF 4A	LSR	A	; YES - TRANSFORM RESULT TO MATCH
A2C0 08	PHP		; DIVIDE EXP BY 2
A2C1 18	CLC		; SAVE CARRY (LSB OF DIGRT)
A2C2 69 40	ADC	##\$40	
A2C4 85 E0	STA	FR1	
A2C6 A9 01	LDA	#1	
A2C8 28	PLP		; MANTISSA = 1
A2C9 90 02	BCC	SQR2	; RELOAD CARRY (LSBIT OF DIGRT)
A2CB A9 10	LDA	##\$10	; WAS EXP ODD OR EVEN
A2CD	SQR2		; ODD - MANT = 10
A2CD 85 E1	STA	FR1+1	
A2CF 20 DB DA	JSR	FMUL	; SQR(X) = SQR(X/100**N) * (10**N)
A2D2	SABSV		; FRO <- ABSVAL(FRO) AC-FRO
A2D2 A5 D4	LDA	FRO	
A2D4 29 7F	AND	##\$7F	
A2D6 85 D4	STA	FRO	
A2D8	SABRTN		
A2DB 60	RTS		

COLLEEN FLOATING POINT ROUTINES BY C SHAW

THE FOLLOWING ROUTINES ARE CALLED BY THE PREVIOUS ROUTINES
 IN GENERAL, THEY DO A 2-LEVEL RETURN WITH CARRY SET IF AN
 ERROR OCCURS, THUS BYPASSING THE REMAINDER OF THE CALLING ROUTINE

A2D9	FSTIR			; LIKE FSTOR EXCEPT USES FR1
A2D9 B4 FC		STX	FLPTR	
A2D9 B4 FD		STY	FLPTR+1	
A2D9 A0 05		LDY	#5	
A2DF	FSLOP			
A2DF B9 E0 00		LDA	FR1,Y	
A2E2 91 FC		STA	(FLPTR),Y	
A2E4 B8		DEY		
A2E5 10 FB		BPL	FSLOP	
A2E7 60		RTS		
A2EB	L01MUL			; FRO <- FRO * DATA CONSTANT (ADDR IN X & Y)
A2EB 20 98 DD		JSR	FLD1R	
A2EB 4C F1 A2		JMP	SFMUL	
A2EE	SQUSR			
A2EE 20 B6 DD		JSR	FMOVE	; FRO <- FRO * FRO
A2F1	SFMUL			; FRO <- FRO * FR1
A2F1 20 DB DA		JSR	FMUL	
A2F4 B0 16		BCS	CRY SND	
A2F6 60		RTS		
A2F7	SFADD			; FRO <- FRO + FR1
A2F7 20 66 DA		JSR	FADD	
A2FA B0 10		BCS	CRY SND	
A2FC 60		RTS		
A2FD A9 01	ONESUB	LDA	#1	; FRO <- 1-FRO
A2FF	INTSUB			; FRO <- A - FRO
A2FF 4B		PHA		
A300 20 B6 DD		JSR	FMOVE	
A303 6B		PLA		
A304 20 53 A3		JSR	PSETO	; A MUST BE FROM 0-9 OR BCD
A307	SFSUB			; FRO <- FRO - FR1
A307 20 60 DA		JSR	FSUB	
A30A	CRYCHK			; CHECK CARRY TO SEE IF THERE IS AN ERROR
A30A 90 02		BCC	RETURN	; RETURN IF CARRY CLEAR
A30C	CRY SND			; DO A 2-LEVEL RETURN IF ERROR
A30C 6B		PLA		
A30D 6B		PLA		
A30E 60	RETURN	RTS		
A30F	L01DIV			; FRO <- FRO / (X,Y)
A30F 20 98 DD		JSR	FLD1R	
A312	RFDIV			; FRO <- FRO / FR1
A312 20 28 DB		JSR	FDIV	
A315 B0 F5		BCS	CRY SND	
A317 60		RTS		

COLLEEN FLOATING POINT ROUTINES BY C SHAW

A319	RENTED			; FRO <- INT(FRO)
A31B A5 D4		LDA	FRO	
A31A 4B		PHA		
A31F 20 31 A3		JSR	STRUNC	; FRO <- TRUNC(FRO), RETURN EQ IF ALREADY INT
A31E F0 2F		BEQ	INTRT3	; INTEGER POP AND RETURN
A320 6B		PLA		; RELOAD OLD FRO WITH SIGN
A321 10 2D		BPL	INTRT2	; POSITIVE
WAS NEGATIVE NON-INTEGER				
A323	SUBONE			; FRO <- FRO-1
A323 A9 01		LDA	#1	
A325	SUBINT			; FRO <- FRO - A
A325 20 FF A2		JSR	INTSUB	; FRO <- A-FRO
A328	SCH050			
A328 A5 D4		LDA	FRO	; FRO<- -FRO AC-FRO SET EQ/NE
A32A F0 04		BEQ	SCH10	
A32C 42 B0		eor	##\$80	
A32E 85 D4		STA	FRO	
A330	SCH10			
A330 60		RTS		

COLLEEN FLOATING POINT ROUTINES BY C SHAW

GREATEST INT <= FRO

PART OF INT ROUTINE FROM SHEP ATARI BASIC B0D5-B0EE
DOES NOT AFFECT FR1?

A331	STRUNC		; TRUNCATE FRO RETURN A=0 AND EQ IF FRO WAS ALREADY AN INTEGER
A331 A5 D4	LDA	FRO	; GET EXPONENT
A333 29 7F	AND	#\$7F	; AND OUT SIGN BIT
A335 3B	SEC		
A336 E9 3F	SBC	#\$3F	; GET LOCATION OF 1ST FRACTION BYTE
A338 10 02	BPL	XINT1	; IF >= 0 THEN BRANCH
A33A A9 00	LDA	#0	; ELSE SET =0
A33C	XINT1		
A33C AA	TAX		; PUT IN X AS INDEX INTO FRO
A33D A9 00	LDA	#0	; SET ACCUM TO ZERO FOR ORING
A33F AB	TAY		; ZERO Y
A340	INT2		
A340 E0 05	CPX	#FPREC-1	; IS D.P. LOC >= 5?
A342 B0 07	BCS	INTRTN	; IF YES, LOOP DONE
A344 15 D5	ORA	FRO+1, X	; OR IN THE BYTE OF MANTISSA
A346 94 D5	STY	FRO+1, X	; ZERO BYTE
A348 E8	INX		; POINT TO NEXT BYTE
A349 D0 F5	BNE	INT2	; JMP
A34B	INTRTN		
A34B 48	PHA		; SAVE OR OF ALL FRACTIONAL BYTES
A34C 20 00 DC	JSR	NORM	; NORMALIZE
A34F	INTRT3		
A34F 68	PLA		; RELOAD
A350 60	INTRT2	RTS	
A351	PCLR0		
A351 A9 00	LDA	#0	; CLEAR FRO RETURN WITH CARRY CLEAR (CC)
A353	PSETO		
A353 48	PHA		; SET FRO TO INTEGER PASSED IN A (MUST BE BCD OR <10)
A354 20 44 DA	JSR	ZFRO	RETURN WITH CARRY CLEAR (CC)
A357 68	PLA		
A358 F0 06	BEQ	CLRTN	; FRO <- 0
A35A 85 D5	STA	FRO+1	; 0 => ALL 0'S
A35C A9 40	LDA	#\$40	
A35E 85 D4	STA	FRO	; SET EXPONENT
A360	CLRTN		
A360 1B	CLC		
A361 60	RTS		

COLLEEN FLOATING POINT ROUTINES BY C SHAW

FIND ROUTINES

A362	SINLD		
A362 A2 DF		LDX #PI2	; LOAD 2*PI
A364 A0 A3		LDY #PI2/256	
A366 A3 FB		LDA RADFLG	
A368 F0 A0		BEG SNMOD3	
A36A A2 E5		LDX #C360	; DEGREES => LOAD 360
A36C A0 A3		LDY #C360/256	
A36E	ENDRD		
A36E A0		RTS	
A36F	SINRD		
A36F A3 D4		LDA FRO	
A371 29 7F		AND #\$7F	
A373 C9 43		CMP #\$45	
A375 90 95		BCS CRY SND	; OUT OF RANGE -- 2-LEVEL RETURN
A377 A2 E6		LDX #FPSCR	; SAVE IN TEMP SCRATCH REG
A379 A0 05		LDY #FPSCR/256	
A37B 20 A7 DD		JSR FSTOR	
A37E 20 62 A3		JSR SINLD	; LOAD 2*PI OR 360
A381 20 9B DD		JSR FLD1R	
A384 20 12 A3		JSR SFDIV	; ANGLE/360
A387 20 1B A3		JSR SINTEG	; INT(ANGLE/360)
A38A 20 62 A3		JSR SINLD	; LOAD 2*PI OR 360
A38D 20 98 DD		JSR FLD1R	
A390 20 F1 A2		JSR SFMUL	; INT(ANGLE/360)*360
A393 20 B6 DD		JSR FMOVE	
A396 A2 E6		LDX #FPSCR	; RELOAD ANGLE
A395 A0 05		LDY #FPSCR/256	
A397 20 B9 DD		JSR FLDOR	
A39D 4C 07 A3		JMP SFSUB	; ANGLE - INT(ANGLE/360)*360
A3A0	RIOVL		
A3A0 A9 CD		LDA #RADPI2	; LOAD X & Y REGS IN PREPARATION FOR LOADING REG 0 OR 1 WITH PI/2, 90 OR 100(IF GRAD)
A3A2 1B		CLC	
A3A3 65 FB		ADC RADFLG	
A3A5 AA		TAX	
A3A6 A0 A3		LDY #RADPI2/256	
A3A8 60		RTS	

COLLEEN FLOATING POINT ROUTINES BY C SHAW

DATA

A3A9 40 01 00	ONE	BYTE	\$40, \$01, 0, 0, 0	1
A3AC 00 00 00				
A3AF	SCDEF			
A3AF BD 03 95		BYTE	\$BD, \$00, \$55, \$14, \$99, \$09, -00000355149999	
A3B2 14 99 33				
A3B5 3E 01 60		BYTE	\$3E, \$01, \$60, \$44, \$27, \$52, 0, 000160442752	
A3B8 44 27 52				
A3B8 BE 46 B1		BYTE	\$BE, \$46, \$B1, \$75, \$43, \$55, -008881754355	
A3B8 75 43 55				
A3C1 3F 07 96		BYTE	\$3F, \$07, \$96, \$92, \$62, \$09, 0, 0796926239	
A3C4 92 62 39				
A3C7 BF 64 57		BYTE	\$BF, \$64, \$57, \$64, \$06, \$67, -8457640867	
A3CA 64 08 67				
A3CD 40 01 57	RADPI2	BYTE	\$40, \$01, \$07, \$07, \$96, \$32, P1/2 = L 570796327 PART OF SCDEF	
A3D0 07 96 32				
A3D0 40 90 00		BYTE	\$80, \$90, 0, 0, 0, 0	140 (DEGREES)
A3D6 00 00 00				
A3D9 3F 01 7A	PIINV	BYTE	\$3F, \$01, \$7A, \$53, \$29, \$29, P1/180 = 0174532925 DEG-2RAD	
A3DC 53 29 25				
A3DE 40 06 2E	E12	BYTE	\$40, \$06, \$2E, \$31, \$85, \$31, L2#P1 = A 28318531	
A3E2 31 85 31				
A3E5 41 03 60	COHD	BYTE	\$41, \$03, \$60, 0, 0, 0	1360
A3EB 00 00 00				
BFEA 00 A0	WORD	START	CARTRIDGE START INFO	
BFFC 00 04	BYTE	0, 4	COLD/WARM START ADDRESS	
BFFE CD A0	WORD	INTT	RUN CARTRIDGE	
	END		POWER UP START VECTOR	

COLLEEN FLOATING POINT ROUTINER BY C SHAW

	SYMBOL	TABLE						
APP	D600	A201	A202	ATAN2	A233	ATCOEF	DFAE	
ATNOUT	A20E	C360	A0E5	C10V	E456	CIX	00F2	
CLRTN	A360	CONTIN	A032	CR	0098	CRYCHK	A30A	
CRY SND	A30C	DIGIT	00F1	EEXP	00ED	ERRMSG	A079	
B SIGN	00EF	EXP	00C0	EXP1	DE03	EXP10	DDCC	
EXP11	DE12	FADP	D486	FASC	D8E6	FASC2	D905	
FCHRFL	00F0	FDIV	D92B	FHALF	DF6C	FLDOR	DB89	
FLD1R	DD98	FLPTR	00FC	FMOVE	DDB6	FMUL	DADB	
FMS	DFEA	FPI	D4D2	FFREC	0006	FPSCR	05E6	
FSCR1	05EC	FPTIR2	00FE	FRO	00D4	FR1	00E0	
FR2	00E6	FR4	00DA	FRX	00EC	FSCR	05E6	
FSCR1	05EC	FSLDH	02DF	FSQR	A25E	FSTOR	DDA7	
FST1R	A2D9	FSUB	DA60	FTEMP	0482	GETNUM	A04C	
GETREC	0005	IGRAL	0144	ICBL	0348	ICCOM	0342	
IFP	D9AA	INBUFF	00F3	INIT	A0CD	INT2	A340	
INTFLG	0481	INTLBF	DA51	INTRT2	A350	INTRT3	A34F	
INTRTN	A34B	INTSUB	A2FF	LBPR1	057E	LBPR2	057F	
LBUFF	0580	LD1DIV	A30F	LD1MUL	A2E8	LOG	DEC0	
LOG10	DEDI	LOGLOC	DEB9	LOGCHK	A15E	LOGCLP	A167	
MLOOP	A01D	NATCF	000B	NOERR	A018	NORM	DC00	
NSCF	0006	NSIGN	00EE	ONE	A3A9	ONESUB	A2FD	
PCLRO	A391	PERR2	A150	PERROR	A14F	PI2	A3DF	
PIOV18	A3D9	PIOV4	DFF0	PIOVL	A3A0	PLYARG	05E0	
PLYEV1	DD40	PRTN	A151	PSETO	A353	PULRTN	A176	
PUTREC	0009	QUADFL	0480	RADFLG	00FB	RADPI2	A3CD	
RETURN	A30E	RTURN2	A178	SABRTN	A2DB	SABSVA	A2D2	
SATAN	A1E4	SCH10	A330	SCHGSG	A328	SCDEF	A3AF	
SCOS	A179	SEXPOS	A0BD	SEXP10	A0C9	SEXPE	A07F	
SEXPT1	A0B6	SFADD	A2F7	SFDIV	A312	SFER3	A00C	
SFMUL	A2F1	SFSUB	A307	SINF3	A1B2	SINF4	A1D4	
SINFIN	A1E3	SINFN2	A1E2	SINLD	A362	SINMOD	A36F	
SINTEG	A318	SLN	A152	SLOGTE	A158	SNMOD3	A36E	
SP0W10	A0DC	SP0W20	A0DF	SP0W50	A109	SP0W80	A140	
SPOWER	A0CE	SQR2	A2CD	SQRDON	A2AC	SQRERR	A23F	
SQRLP	A275	SR0U10	A13A	SSIN	A185	SSQRT	A241	
SQSQR	A2EE	START	A000	STRUNC	A331	SUBINT	A325	
SUBONE	A323	XCVFRO	DC70	XEFORM	D920	XEfrm2	D928	
XFORM	DE95	XINT1	A33C	ZF1	DA46	ZFR0	DA44	
ZTEMP1	00F5	ZTEMP3	00F9	ZTEMP4	00F7			